

Feynman integrals

(a)

$$\frac{1}{A_1 \dots A_n} = \int_0^1 dx_1 \dots dx_n \frac{\delta(\sum x_i - 1)}{(x_1 A_1 + \dots + x_n A_n)^n} \quad (n-1)!$$

in particular

$$\frac{1}{ab} = \int_0^1 dx \frac{1}{(\alpha a + (1-\alpha)b)^2}$$

$$\int \frac{d^d k}{(2\pi)^d} \frac{1}{(k^2 - \Delta)^n} = \frac{(-)^n i}{(4\pi)^{d/2}} \frac{\Gamma(n-d/2)}{\Gamma(n)} \frac{1}{\Delta^{n-d/2}}$$

$$\int \frac{d^d k}{(2\pi)^d} \frac{k^2}{(k^2 - \Delta)^n} = \frac{(-)^{n-1} i}{(4\pi)^{d/2}} \frac{d}{2} \frac{\Gamma(n-d/2-1)}{\Gamma(n)} \frac{1}{\Delta^{n-d/2-1}}$$

$$\Gamma\left(\frac{\epsilon}{2}\right) = \frac{2}{\epsilon} - \gamma + \dots$$