

# The Sports Product Market

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ECONOMICS OF SPORTS (ECON 325)

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# What kind of good is sports?

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- All goods can be classified according to the combination of 2 properties they have (or don't):
  - Rivalry in consumption and
  - Excludability.
- Sports defined how?
  - Admission as spectator: excludable and non-rival, until SRO sells out at least.
  - Broadcasts, “accounts and descriptions of this game . . . .”: excludable in principle and non-rival.
    - But difficult to enforce, practically non-excludable.
  - Merchandise: excludable and rival, a private good.
- Tickets to most games and legal broadcasts of games are “natural monopolies” or “club goods” like toll roads or gated internet content.
- Most other forms are essentially public goods like fireworks displays or national defense.
  - Hard to stop me from playing fantasy baseball using MLB’s stats, even if they wanted to.
    - Schwarz, Alan. 2004. The Numbers Game. St. Martin’s, New York. 173-194.

# Leagues and clubs

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- Who is making the choices?
  - Individual clubs.
  - But some coordination with other clubs, restrictions by the league.
- Do the clubs do collectively what a planner in charge of the whole league would do?
  - I.e., price to maximize overall profit, like an economic firm.\*
  - Also pay and allocate players to maximize overall profit.
- Do the sports clubs behave like firms, even with respect to maximizing *their own* profits?
  - Even if their collective choices don't maximize overall league profit.

\* [See](#) Neale, Walter. 1964. "The Peculiar Economics of Professional Sports." *The Quarterly Journal of Economics*: Vol.78, No. 1, 1-14.

# Clubs' objectives

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- Profit (“ $\pi$ ”): Ferguson et al. ([1991](#))
- Wins
  - Subject to some kind of break even constraint.
  - Maybe an “acceptable (\$) losses” constraint if owners get consumption value from their team’s performance: Sloane ([1971](#)),
- A combination of profit and wins
- Fans’ utility: Madden ([2012](#))
- Zimbalist’s ([2003](#)) literature review
  - See references for papers that test

# If clubs maximize profits on ticket sales

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- They solve:

$$\max \pi = pA - C ,$$

Where  $p$  is price,  $A$  is attendance, and  $C$  is the club's total costs per game.

- As a monopolist facing a downward-sloping demand curve,  $A$  is a function of  $p$ .
- To maximize profit, the club solves the maximization problem with the first order condition:

$$\frac{d\pi}{dp} = p \frac{dA}{dp} + A - \frac{dC}{dA} \frac{dA}{dp} = 0.$$

- And this is even simpler if one assumes that the marginal cost of another fan is zero.

$$\frac{dC}{dA} = 0 \rightarrow p = -A \frac{dp}{dA}.$$

# If clubs maximize profit on ticket sales

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- Simplifying this results in a simple pricing rule:

$$\frac{p}{p} = \frac{A dp}{p dA}; 1 = |\varepsilon|; \varepsilon \equiv \text{demand elasticity.}$$

- If the club is on an elastic ( $|\varepsilon| > 1$ ) part of the curve, it should cut prices and increase revenue through higher attendance.
  - If it's on an inelastic ( $|\varepsilon| < 1$ ) part, it should raise prices and increase revenue; not very many fans will be dissuaded.
  - And stop changing prices when they get to the point where demand is unit elastic.
- Obviously if the capacity of the stadium is less than the optimum implied above, they would only cut price to the point of a sellout.

# Implications

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- The club does not price at marginal cost (\$0/person).
  - Some fans who are willing to pay more than marginal cost would be denied tickets.
- Fixed costs, like player payroll, do not enter into the optimal ticket price.
- Although it impacts the club's decisions about hiring players, trying to maximize other things, like wins, should not affect the ticket pricing behavior.
  - A better team would shift demand for tickets outward, but taking that new curve as given, the unit elasticity rule still applies.
  - Opponents that attract more fans or games on weekends should have higher prices, if clubs price according to this rule.

# Limitations

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- Single price, no price discrimination.
- No differentiation of sections within the stadium (“homogenous” tickets).
- No other sources of revenue accounted for.
  - In a simplistic way, this is easy to relax.



# Broadcasting rights

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- Significant revenue comes from excluding all but the buyer of the rights from broadcasting games.
  - Again some teams' games have larger viewing audiences (and ticket-buying audiences).
- Teams could sell individually or the league could sell the rights collectively.
  - The latter saves on transaction costs of repeated negotiation and gives the league more bargaining power, Falconieri, et al. ([2004](#)).
  - Revenue sharing across teams is another motivation for, but is not unique to, collective selling.
  - Weaker teams might free-ride because revenue depends only on *league* performance.

# Investing in talent, given optimal pricing

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- But where does the broadcast revenue go? Baseline case: clubs get, and try to maximize, their broadcast revenue.
  - But differ in market size.
  - Follow Falconieri, et al., here.

$$R_i = A_i \left( \frac{t_i}{t_i + t_{-i}} \right) (1 + \kappa_i); t_i \text{ is team } i\text{'s talent level.}$$

- The big parenthesis is team  $i$ 's strength and winning probability. Think of this as a shifter of the team's demand curve and the ability to choose a higher  $p^*$ .
- $\kappa_i$  is the broadcast revenue multiplier, and it's bigger for larger market clubs.
- Talent, of course, is costly, and clubs have to pay to shift their demand curves out.

$$C_i = ct_i + c_i^0.$$

# Investing in talent, continued

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- Clubs maximize profit by choosing how much talent to invest in:

$$\pi_i = A_i \left( \frac{t_i}{t_i + t_{-i}} \right) (1 + \kappa_i) - ct_i - c_i^0; \frac{d\pi}{dt_i} = A_i(1 + \kappa_i) \left[ \frac{1}{t_i + t_{-i}} - \frac{t_i}{(t_i + t_{-i})^2} \right] - c = 0.$$

- Equilibrium would mean solving “n” (1 per club) of these conditions simultaneously for the vector,  $\mathbf{t} = [t_1^* \dots t_n^*]$  (Falconieri, et al., p. 842).

# Investing in talent, continued

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- “Despite all the simplifying assumptions built into the model, in general, we cannot solve this system explicitly” – the authors. So rather than banging your head against a wall, recognize that the square brackets can be expressed in terms of team  $i$ 's relative strength (win probability):

$$\left[ \frac{1}{t_i + t_{-i}} - \frac{t_i}{(t_i + t_{-i})^2} \right] = \frac{t_{-i}}{(t_i + t_{-i})^2} = \frac{1 - w_i}{t_i + t_{-i}}.$$

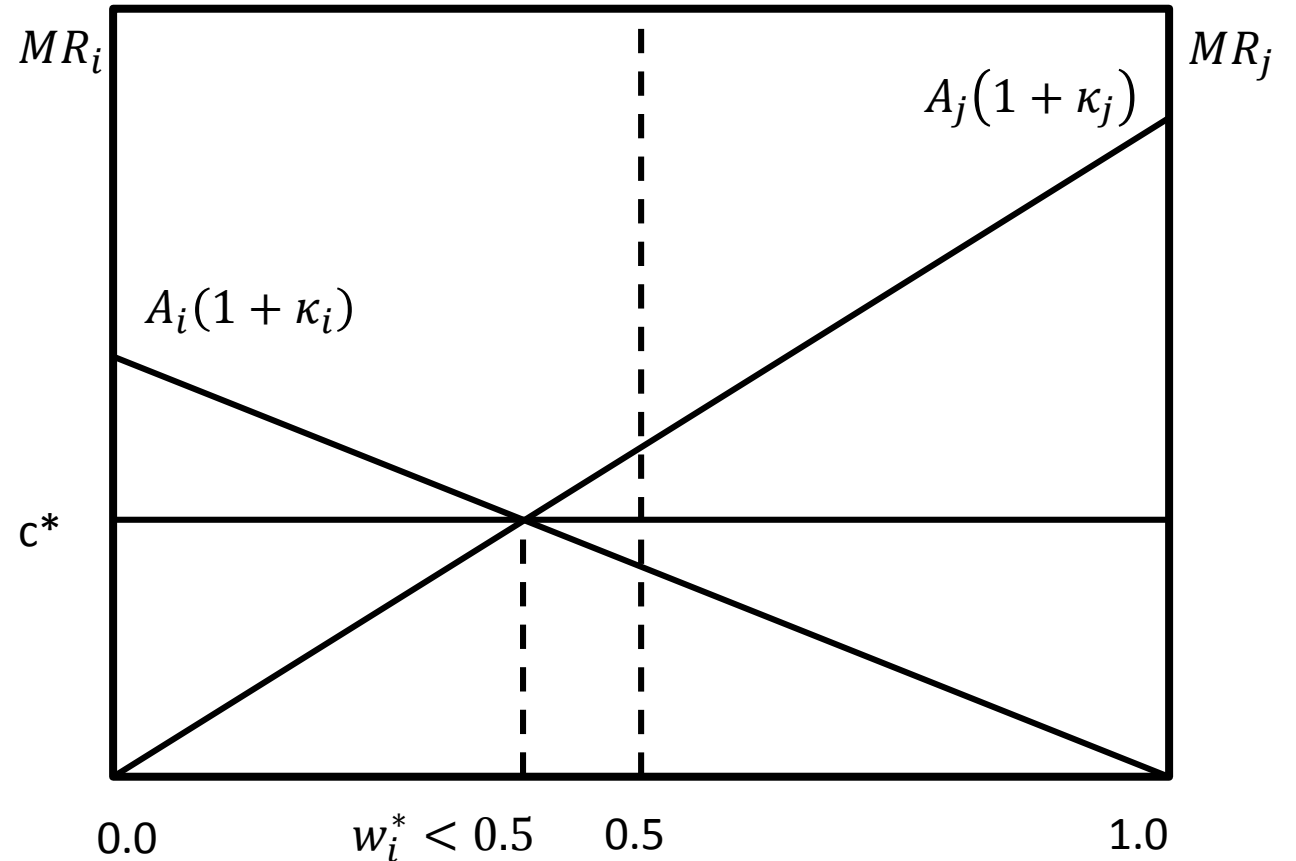
- This simplifies down to  $(1 - w_i)$ , if you normalize the total talent to 1.
- so you could draw any club's marginal revenue function as a downward sloping line.

# Investing in talent, equilibrium characterized

MR for a bigger market club is strictly higher than for a smaller club.

- Competition bids the price of talent up to the point ( $c^*$ ) at which all (or both, in the simplified 2 team league picture) clubs marginal revenues are equal.
- If any club's MR were to exceed  $c^*$ , it would either outbid other clubs or bid up  $c$ , thus not equilibrium.

In equilibrium the talents and winning %s deviate from the balanced ( $0.5 \forall i, j$ ) outcome.



→ Pr(Team i win) ; Pr(Team j win) decreasing.

# (broadcast) Revenue sharing

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This is where it gets fun.

The league can manipulate this equilibrium by dividing the revenue “ $v$ ” from the collective sale of broadcasting rights:

- Equally among all teams, or
- Based on performance.

Equal sharing just means replacing the private revenue with the club’s share of collective revenue:

$$R_i = A_i \left( \frac{t_i}{t_i + t_{-i}} \right) + \frac{v}{n}$$

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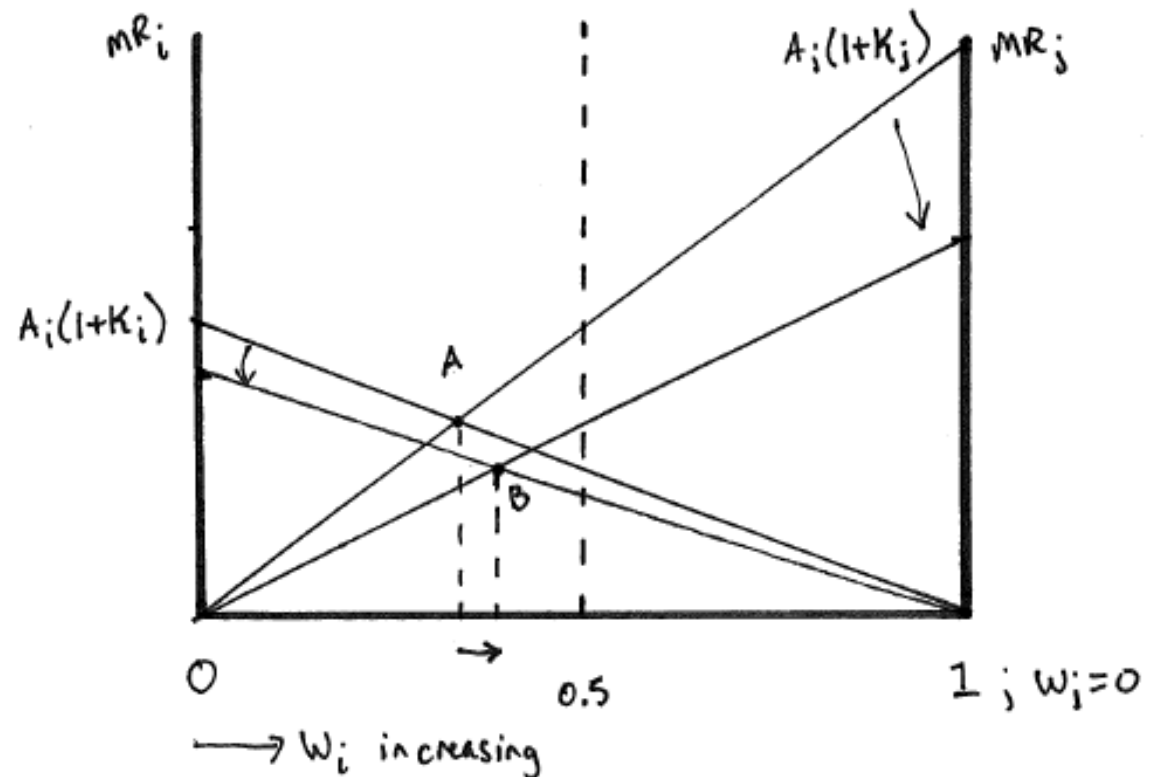
# Equal sharing

Sharing of broadcast revenue takes the broadcast audience out of the clubs' MRs.

- This diminishes the advantage of the bigger club(s).
- But they still have a MR advantage via ticket sales.

You get closer but not all the way to perfect competitive balance.

- Unless there is a sufficiently large prize (Falconieri, et al., p. 845), on top of local ticket revenue, for winning.



# Equal sharing, caveats

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Investment in talent is lower because clubs cease to take into account their effects on “ $v$ ”.

- The free rider effect.

In terms of *total* revenue, this could get offset by a bargaining power effect.

- The league is a monopolist now that could extract more of the surplus from the sale to broadcasters.

Also (though it is not modeled here) competitive balance *may* have a net positive effect on  $v$ .

- The league gets more popular overall because the games are closer/more uncertain.



# Performance-based sharing

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Equal sharing is a special case of this scenario, under which the league can designate a fraction of  $v$ ,  $(\theta)$ , to go to clubs based on performance.

- Obvious to see why this *would* increase the incentive to invest in talent.

Revenue is:

$$R_i = A_i(1 + \theta v) \left( \frac{t_i}{t_i + t_{-i}} \right) + \frac{(1 - \theta)v}{n}$$

MR increases for both clubs and so does the equilibrium investment in talent.

Competitive balance in equilibrium is less clear.

# Performance-based sharing, continued

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This is where it's important to consider clubs' effects on the league broadcast revenue.

- If they completely ignore this, because their slice of the pie is so small ( $1/n$ ), competitive balance is the same as under equal sharing.
- Big and small market clubs proportionally increase their investments in talent, leaving the ratios unchanged.
- Or even if they *do* consider this, but in the identical way so:  $\frac{dv}{dt_i} = \frac{dv}{dt_j} \forall i, j$ .

But if big clubs have a (and recognize their) bigger effect on the “size of the pie,” they invest proportionally more in talent (like private sale), and balance is worse.

- More will tune in to see a big club in the championship?

# Performance-based sharing, continued

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Or the opposite could be the case if big (small) clubs recognized their negative (positive) effect on balance and invested proportionally less (more).

- In 2016 people actually tune in to watch their team play the Kansas City Royals!
- Conversely fans are reluctant to watch their home team get whopped by the “Yankees” yet again.

This is called the rent-seeking effect by Falconieri, et al., the added incentive to win created by revenue sharing.

- It gets larger, the larger is the league’s bargaining power effect. Assuming  $\theta > 0$ .

# Performance-based sharing is a substitute for a large prize (“z”)

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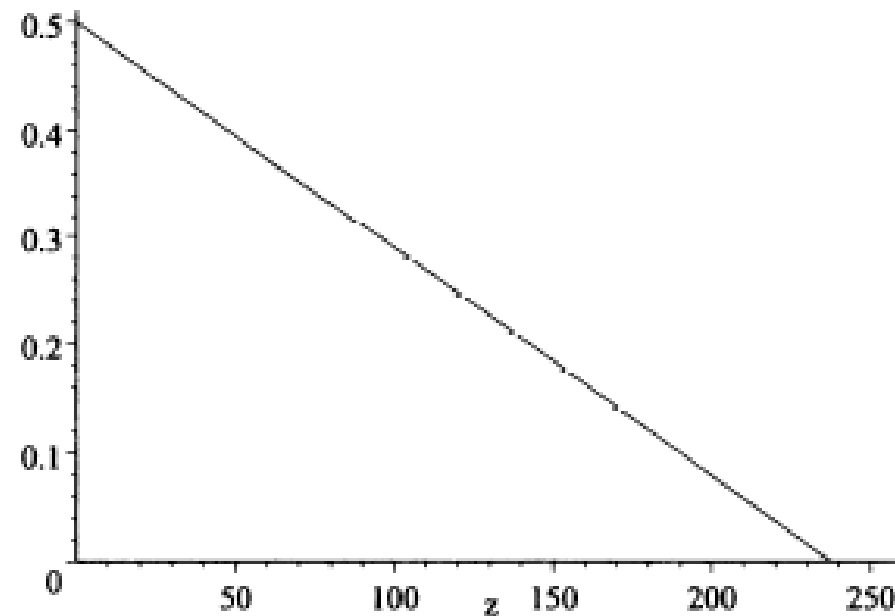


FIGURE 2. The optimal level of revenue sharing ( $\theta^*$ ) as a function of  $z$ .

# Broadcast rights, empirical literature

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Noll ([2007](#)): collective sale is a bad idea. It doesn't help balance, makes it more expensive to consumers.

- Peeters ([2011](#)) agrees. Even the rent-seeking effect helps stronger drawing teams in the UEFA.

Szymanski ([2001](#)): increases in revenue dispersion have not affected balance.

Vrooman ([2009](#)): autoregressive process estimation to infer competitive balance.

# Demand for tickets

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The population of potential attendees has diverse preferences for going to any given game. Formally this is represented by each person's (indexed by  $i$ ) utility function:

$$U_i = v_i - p; v \equiv \text{person } i\text{'s value placed on attending the game.}$$

Each person will attend if  $U > 0 \rightarrow v_i > p$ .

$v$  is assumed to have a probability distribution in the population, e.g., uniform, normal, exponential, such that for any  $v_i$ ,  $F(v_i) = \Pr(v \leq v_i) \in [0,1]$  gives the share of people who value attendance less than or equal than person  $i$  does.

For a population of  $N$  people, when the club sets price  $p$ , the quantity that will demand tickets is:

$$A = [1 - F(p)] * N; \text{ since } \frac{dF}{dp} > 0,$$

this quantity falls with  $p$ . As the Law of Demand would predict. [Back](#).

# Extension: non-ticket revenue is proportional to attendance.

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If the proportionality is  $\kappa$ , profit is:

$$\pi = (p + \kappa) * A(p) - C.$$

The maximum implies:

$$A + (p + \kappa) \frac{dA}{dp} \rightarrow 1 - \frac{\kappa}{p} = -\frac{1}{\varepsilon}; \varepsilon^* = \frac{p}{p + \kappa} < 1,$$

i.e., optimal ticket pricing in the inelastic region of the demand curve.

[Back.](#)