

# Discrimination: Second Lecture

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LABOR ECONOMICS (ECON 385)

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# Introduction

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- Statistical Discrimination. Preferences are not the only mechanism through which discrimination occurs. Alternatively, information asymmetries can lead to discrimination.
- Employers attempt to use salient traits like gender to signal an applicant's labor force attachment or productivity.
- Consider the following model of discrimination.\*

\*Based on Aigner, Dennis J. and Glen G. Cain. 1977. "Statistical Theories of Discrimination in Labor Markets." *Industrial and Labor Relations Review*, Vol. 30, No. 2: 175-187.

# The model

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- There are two groups of workers, “Male” and “Female”. They submit accurate (but imprecise or “noisy”) signals (“ $y$ ”) of their productivity (“ $q$ ”) to employers:

$$y = q + u,$$

where the term,  $u$ , reflects the signal’s imprecision; think of a thorough “resume” as the signal.

# The model, continued

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Employers base their wage offers on the expected value of  $q$ , conditional on the observed signal,  $y$ :

$$E(q|y) = \text{wage} = \hat{q}.$$

- Each group can have a different average productivity ( $\alpha_M$  and  $\alpha_F$ ), a different variance in productivity ( $\text{Var}(q_M)$  and  $\text{Var}(q_F)$ ), and different precision in signals ( $\text{Var}(u^M)$  and  $\text{Var}(u^F)$ ).
- Claim: based on the signal,  $y$ , the expected value of  $q$  is a weighted average of the signal and the group's mean productivity.

$$E(q|y, M) = (1 - \gamma^M)\alpha^M + \gamma^M y$$

$$E(q|y, F) = (1 - \gamma^F)\alpha^F + \gamma^F y$$

- Gamma ( $\gamma$ ) is the weight, determined by,

$$\gamma = \frac{\text{Covariance}(q, y)}{\text{Var}(y)}.$$

# The model, continued

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- The weights depend on what fraction of signal variation comes from productivity differences and what fraction comes from imprecision, i.e.,

$$\text{Var}(y) = \text{Var}(q) + \text{Var}(u).$$

- The weight placed on the signal is:

$$\gamma = \frac{\text{Var}(q)}{\text{Var}(q) + \text{Var}(u)} = \frac{\text{Cov}(y, q)}{\text{Var}(y)}.$$

- If there was no imprecision, the signal would perfectly reveal productivity, and gamma would equal 1. If the signal was totally uncorrelated with productivity, gamma would be 0.

# Discrimination from poor signal strength

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If the signal is perfect, there is no discrimination between groups; everybody just gets his/her VMP like earlier models. If the signal is really poor, group differences determine wage offers. I.e.,

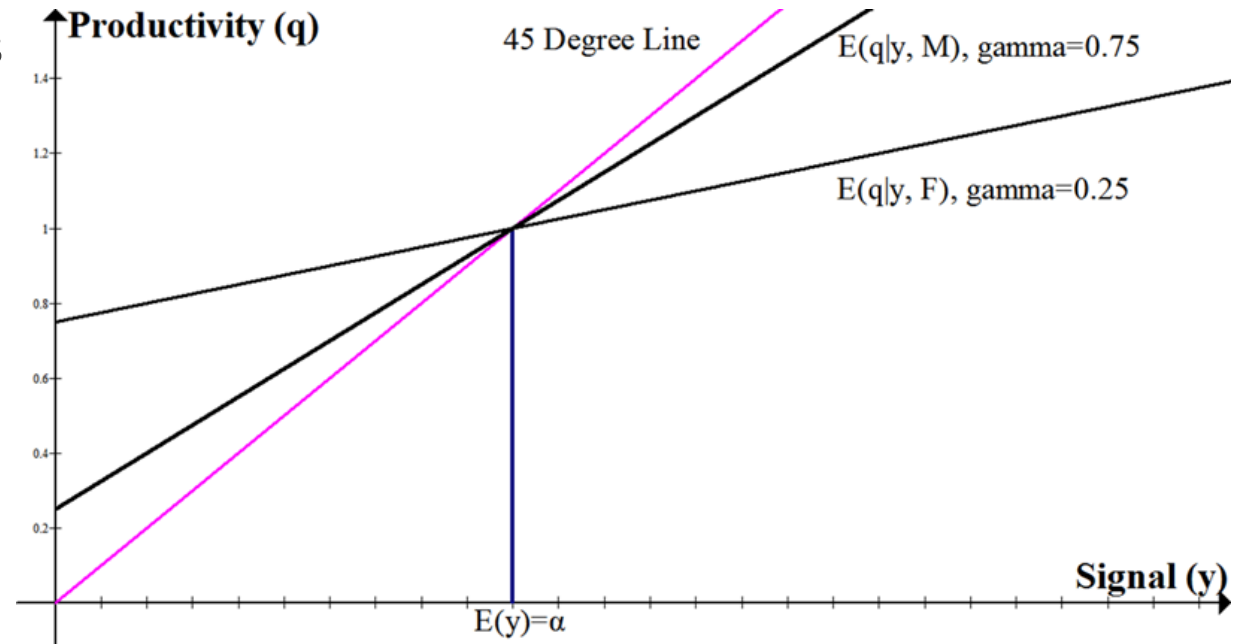
$$\text{Cov}(q, y^M) = \text{Cov}(q, y^F) = \gamma^M = \gamma^F = 0,$$

and  $\hat{q}|M = \alpha^M, \hat{q}|F = \alpha^F$ .

- Discrimination is not based on preferences—instead on lack of information about each individual.
- If the groups have two different average productivity levels, they will still (rightly) have different average wages.
- Even if they have the same average productivity ( $\alpha^M = \alpha^F = \alpha$ ), wages between the groups may differ based on the precision of signals.

# Effect of variation in productivity within groups

- If one group has a larger  $Var(q)$ , it means that a “good” (greatly above average) signal reveals more information.
  - Same with a “bad” (below average) signal.
- If men vary more in their productivity, a “good” signal sent by a man will create a better impression than one sent by a woman.
  - A “bad” signal sent by a man will create a worse impression than one sent by a woman.



# Effect of variation in signal strength

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- If one group has a “noisier” signal ( $Var(u)$  is higher), it produces the same result as the previous graph, with more weight being placed on the signal of the more precise group.
  - But neither of these possibilities explains systematic differences between groups . . . yet. Losses by low productivity men are negated by gains by high productivity men. Resulting in no difference in average wage.



# Extensions to the A&C model

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- Discrimination could result from differences in the productivity variance across groups if the employers care about the variance in addition to the expected value.
  - Hiring would favor the group with less variance.
- If workers with very low  $q$  are not hired at all—instead of hired at a low wage—the model would predict wage gaps in favor of the group with lower (productivity or signal) variance.

# Discrimination coefficient, continued

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- Though the market wage for black workers is  $w_b$ , the employer acts as if it costs  $w_b(1 + d)$  dollars to hire them.
- So they are less likely to hire the cheaper group at all, and even if they do hire them, they will hire fewer of them than is profit-maximizing.
- Note: the “colorblind” firm is included ( $d = 0$ ) as a special case.

# Statistical discrimination

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Incentives for statistical discrimination will exist as long as information about productivity is revealed by non-productive characteristics.

- Better methods for screening applicants based on productivity would remedy.
  - Gets individuals to self-select, separating equilibrium.
  - Arbitrage opportunities exist if a firm can devise [a more accurate way](#) to estimate applicants' productivities. They should respond to this incentive!
- Some advocate more heavy-handed approaches: anti-discrimination, equal pay laws.
  - Economists are reluctant to support these because they don't actually deal with the information problem.