

# ECE 414 – Spring 2016

## Homework #3

Out: 01.21

Due: 01.28

**1. Replacing an arbitrary 'black box' ray matrix with a single lens.** An optical black box has various optical elements inside it, producing a given real ABCD matrix from its input plane to its output plane. We want to replace this black box with a box of physical length  $L$ , containing only a single lens of focal length  $f$ . Can this be done? Why? And if so, what total length  $L$ , focal length  $f$ , and lens location  $x$  (within  $L$ ) will be required?

**2. (Exercise 1.4-6) A Periodic Set of Pairs of Different Lenses.** Examine the trajectories of paraxial rays through a periodic system composed of a set of lenses with alternating focal lengths  $f_1$  and  $f_2$  as shown in the figure below. Show that the ray trajectory is bounded (stable) if

$$0 \leq \left(1 - \frac{d}{2f_1}\right) \left(1 - \frac{d}{2f_2}\right) \leq 1$$

