# Fall 2018 - Mid-Term 1 ECE 301: Signals and Systems

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Last Name :

First Name :

PUID :

#### Instructions.

- Write your full name, PUID on this page
- This is a 50 minute exam containing 5 questions, 30 points each totaling 150 points.
- Please write clearly and legibly
- Your solutions must include detailed steps and/or explanations. Do not simply state the answer
- One A-4 sized crib sheet front and back is allowed.
- There should be 7 pages including the cover page.

Question | Points

The output at time n for a system is obtained by accumulating the values of the input from n+7 to  $\infty.$ 

a What is the impulse response?

b What is y[n] when x[n] = u[n] - u[n - 4], where u[n] indicates unit step.

c Is this system

i Causal?

ii Memoryless?

iii Stable?

iv Invertible? If invertible find the impulse response of the inverse system.

For the following questions, determine if the signals are periodic or not. If periodic, find their fundamental period.

a . $e^{-7jt}$ 

b .  $e^{5jt} + je^{10jt}$ 

c .  $e^{2t}$ 

d . $e^{-2t}u(t)$ 

e . $\cos(7\pi n^3)$ 

f .  $\cos(10\pi t) + \cos(3t)$ 

Calculate  $E_\infty$  and  $P_\infty$  for the following

a  $x[n] = \sin(\frac{\pi}{4}n)$ 

b  $x(t) = e^{j(5t - \frac{\pi}{8})}$ 

c 
$$x[n] = u[n]$$

d  $x[n] = \delta[n]$ 

Find the convolution of the signals given below.

a i 
$$x(t) = u(t)$$
  
ii  $h(t) = e^{-2t}u(t)$ 

b i 
$$x[n] = \delta[n] + \delta[n+1] + \delta[n-2]$$
  
ii  $h[n] = u[n]$ 

a) For the signal x(t) in Figure 1, sketch x(-3t-1)



Figure 1: x(t)

b) Sketch 2u[-n-1] where u[n] is a unit step function