

Fall 2018 - Mid-Term 2  
ECE 301: Signals and Systems

Prof.Aly El Gamal

Last Name :

First Name :

PUID :

**Instructions.**

- Write your full name, PUID on this page
- This is a 50 minute exam containing 5 questions, 30 points each totaling 150 points.
- Please write clearly and legibly
- Your solutions must include detailed steps and/or explanations. Do not simply state the answer
- Two A-4 sized crib sheet front and back is allowed.
- There should be 7 pages including the cover page.

Question	Points
1	
2	
3	
4	
5	
Total	

## Problem 1

For the continuous time periodic signal  $x(t)$  as given below

$$\sum_{k=-\infty}^{\infty} \delta(t - kT)$$

- a Find the Fourier Series coefficients of  $x(t)$ .
- b Find the Fourier Transform  $X(j\omega)$  of  $x(t)$ .
- c Sketch  $x(t)$  when  $T \rightarrow \infty$ .
- d Find the Fourier transform of the signal  $x(t)$  when  $T \rightarrow \infty$ .

## Problem 2

Find the Fourier Transform of the signal  $x(t)$  as shown in figure 1

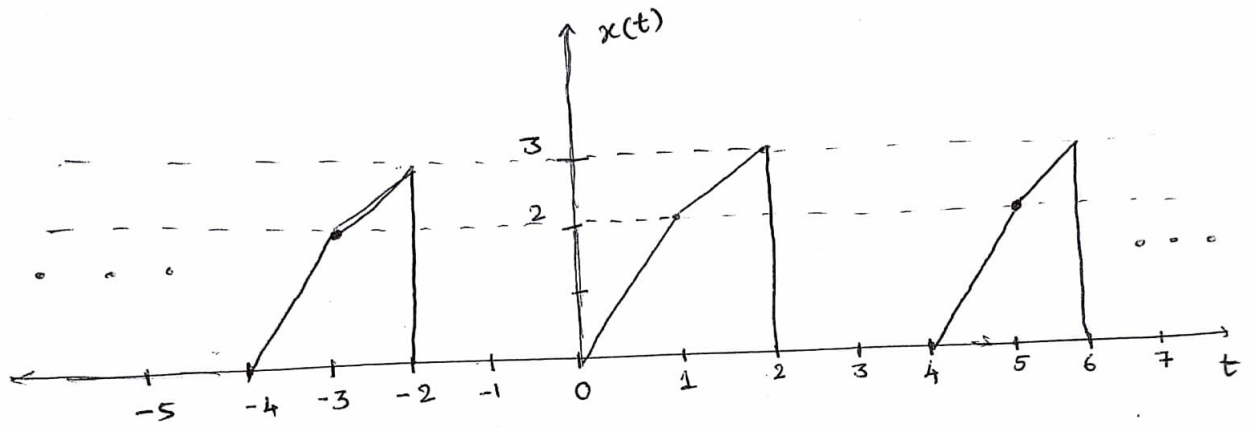


Figure 1:  $x(t)$

### Problem 3

Consider a real periodic signal  $x(t)$  with fundamental period  $T$  and Fourier series coefficients  $a_k$ . Find the following using the given information.

a Fourier Series coefficients of Even part of  $x(t)$ .

b Fourier Series coefficients of Odd part of  $x(t)$ .

c Evaluate  $\sum_{k=-\infty}^{\infty} a_k e^{jk \frac{14\pi}{T}}$

d Evaluate  $\sum_{k=-\infty}^{\infty} (-1)^k a_k$

## Problem 4

Given  $X(j\omega)$  is the Fourier transform of the continuous time signal  $x(t)$ . What is the Fourier transform of the signal  $e^{j\omega_0 t}x(t)$ ?

## Problem 5

Compute the Fourier Series coefficients for the following signal using the multiplication and linearity properties

$$\cos\left(\frac{3\pi n}{4} + \frac{\pi}{4}\right) \sin\left(\frac{3\pi n}{4}\right) + \sin\left(\frac{5\pi n}{3} + \frac{\pi}{4}\right) \cos\left(\frac{5\pi n}{3}\right)$$