

# Fall 2018 - Problem Set 2

## ECE 301: Signals and Systems

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**Due Date : September 28, 2018**

### Intructions

1. Please write clearly and legibly.
2. Your solutions must include detailed steps and/or explanations. Do not simply state the answer.
3. Write your full name(first,last), PUID on your homework submission.
4. All problems carry almost equal weight.

### Problem 1

For each of the below systems with input  $x$  and output  $y$ , determine if they are :

1. Linear or Non linear, 2. Causal or Non causal , 3. Time Variant or Time Invariant, 4.Stable or Unstable

a )  $y[n] = x^2[n]$

b )  $y[n] = 5(n - 1)x[n] + 2$

c )  $y(t) = x(t + 1) \cos(6\pi(t - 1))$

d )  $y(t) = e^{-10t}x(t)$

e )  $y(t) = e^{-10jt}x(t)$

### Problem 2

The output at time  $n$  is obtained by accumulating the values of the input from  $n - 5$  to  $n + 5$ .

- a What is the impulse response?
- b What is  $y[n]$  when  $x[n] = u[n] - u[n - 4]$ , where  $u[n]$  indicates unit step.
- c Is this system
  - i Causal?
  - ii Memoryless?
  - iii Stable?
  - iv Invertible? If so, what is the impulse response of the inverse system.

### Problem 3

- a A discrete LTI system with input  $x_1[n]$  (shown in 1(a)) produces the output  $y_1[n]$ (shown in 1(b)). Find the output produced by this system for the input  $x_2[n]$ (shown in 1(c))
- b A continuous LTI system with input  $x_1(t)$  (shown in 2(a)) produces the output  $y_1(t)$ (shown in 2(b)). Find the output produced by this system for the input  $x_2(t)$ (shown in 2(c))

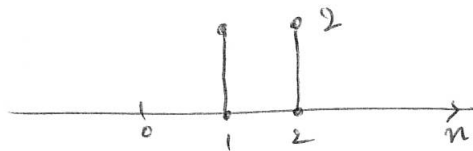


Fig a :  $x_1[n]$

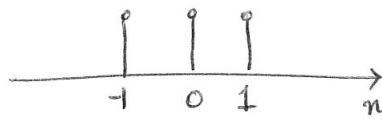


Fig b :  $y_1[n]$

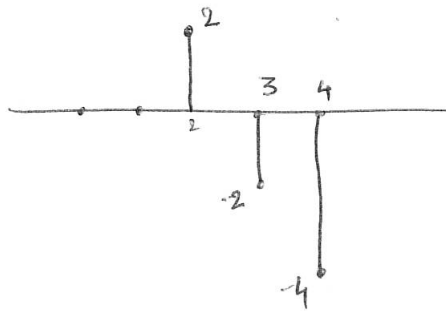


Fig c :  $x_2[n]$

Figure 1

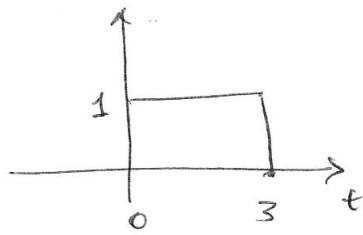


Fig a:  $x_1(t)$ .

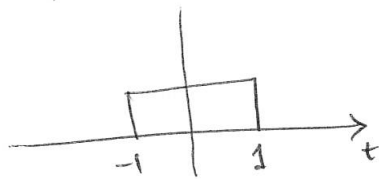


Fig b:  $y_1(t)$ .

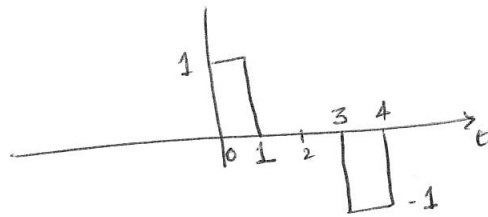


Fig c:  $x_2(t)$ .

Figure 2

## Problem 4

a If  $x(t) * h(t) = y(t)$  where  $*$  indicates convolution, then show that

$$x(t + t_1) * h(t - t_2) = y(t - (t_2 - t_1))$$

b Find  $\int_{-\infty}^{\infty} x(t)\delta(t - t_0)dt$

c Find  $\int_{-\infty}^{\infty} x(\tau)\delta(t + t_0 - \tau)d\tau$

d Find  $\int_{-\infty}^{\infty} x(\tau)\delta(t + \tau)d\tau$

## Problem 5

a For  $x(t)$  and  $y(t)$  in the figure 3, (Note:  $x(t)$  is periodic) find  $x(t) * y(t)$ .

b  $x[n] = \delta[n + 5] + \delta[n - 4] + \delta[n]$

$$y[n] = u[n] - u[n - 2]$$

Find  $x[n] * y[n]$ . Note:  $u[n]$  is unit-step

c Calculate  $x_1[n] * x_2[n] * x_3[n]$ . Note:  $u[n]$  is unit-step

$$x_1[n] = \frac{1}{3}^n u[n]$$

$$x_2[n] = u[n]$$

$$x_3[n] = \delta[n - 2]$$

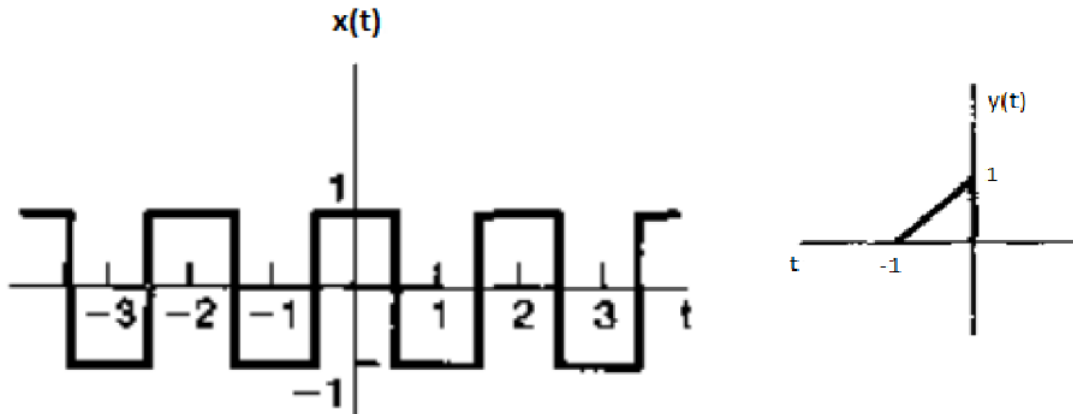


Figure 3